

# Blur Unblurred – a Mini-Tutorial

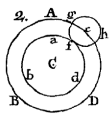
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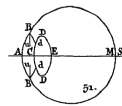
## Summary

- Optical blur from defocus (=dioptric defocus), often confused with low-pass filtering, can occur with myopia, presbyopia or misaccommodation, or purposefully with plus-lenses to study effects of optical degradation.
- Perhaps surprisingly, the dioptric blur kernel is simply a **cylinder**.
- The blur circle's diameter is  $\sim$  pupil size  $\cdot$  defocus. Its size can also be assessed from the near or far point.
- There is a simple formula to derive decimal visual acuity from defocus.

## James Jurin (1738)



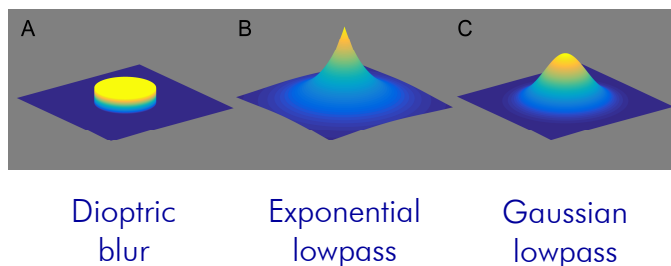
A "circle of dissipation" on a ring stimulus.



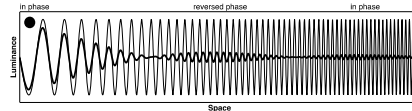
Jurin's eye model for accommodation

To induce blur Jurin proposed bringing a stimulus closer or farther than accommodation allows, and noticed physical blur is not perceptual blur.

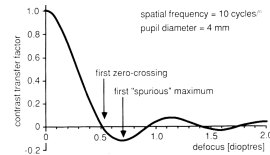
## Blur kernel shapes



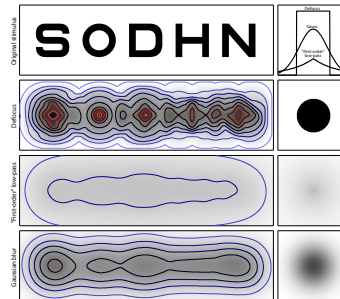
## Spurious resolution



The effect of defocus on a frequency-sweep sine-wave grating.



The contrast transfer factor for a defocused periodic sinusoidal grating. At 0.5 D defocus, contrast is zero.

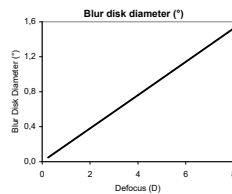
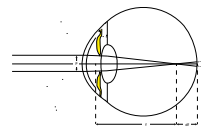


Effect of blur on Sloan letters: original letters and PSFs

Dioptric blur; disk kernel  $\varnothing$  = letter height  
 PSF with exponential drop-off  
 Energy is spread over a wide spatial range

Gaussian blur. Blurred images increased in contrast. Isolumines = luminance steps of 7 %points

## Blur-Disk & pupil size & defocus



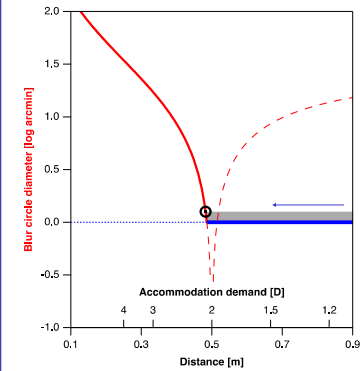
$$b^\circ = 0.057 p_{mm} D$$

$b^\circ$ : blur disk diameter in deg  
 $p_{mm}$ : pupil size in mm  
 $D$ : Defocus in diopters

The derivation is given by Smith (1982a) using the simplified Gullstrand eye. See **separate sheet**.

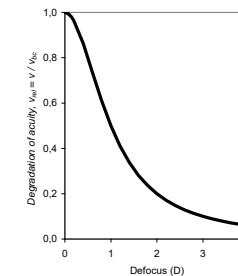
$$b_{stim} = p \left| \frac{d_{foc} - d_{stim}}{d_{stim}} \right|$$

Blur disk in stimulus space when the target is too near or too far.  
 $p$ : pupil size



A target approaching from the right.  
 Blue line: Accommodation  
 Red line: Too near  
 Circle: JND

## Visual acuity & defocus



$$v/v_{bc} = \frac{1}{1 + D^2}$$

$v/v_{bc}$ : Acuity degradation  
 $D$ : Defocus in diopters

$$v/v_{bc} \approx 1 - D^2$$

for small  $D$

**Example:**  
 1dpt decreases acuity to  $\frac{1}{2}$  its value

## References

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 Smith, G. (1982a). Angular Diameter of Defocus Blur Discs. *American Journal of Optometry & Physiological Optics*, 59(11), 885-889.  
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